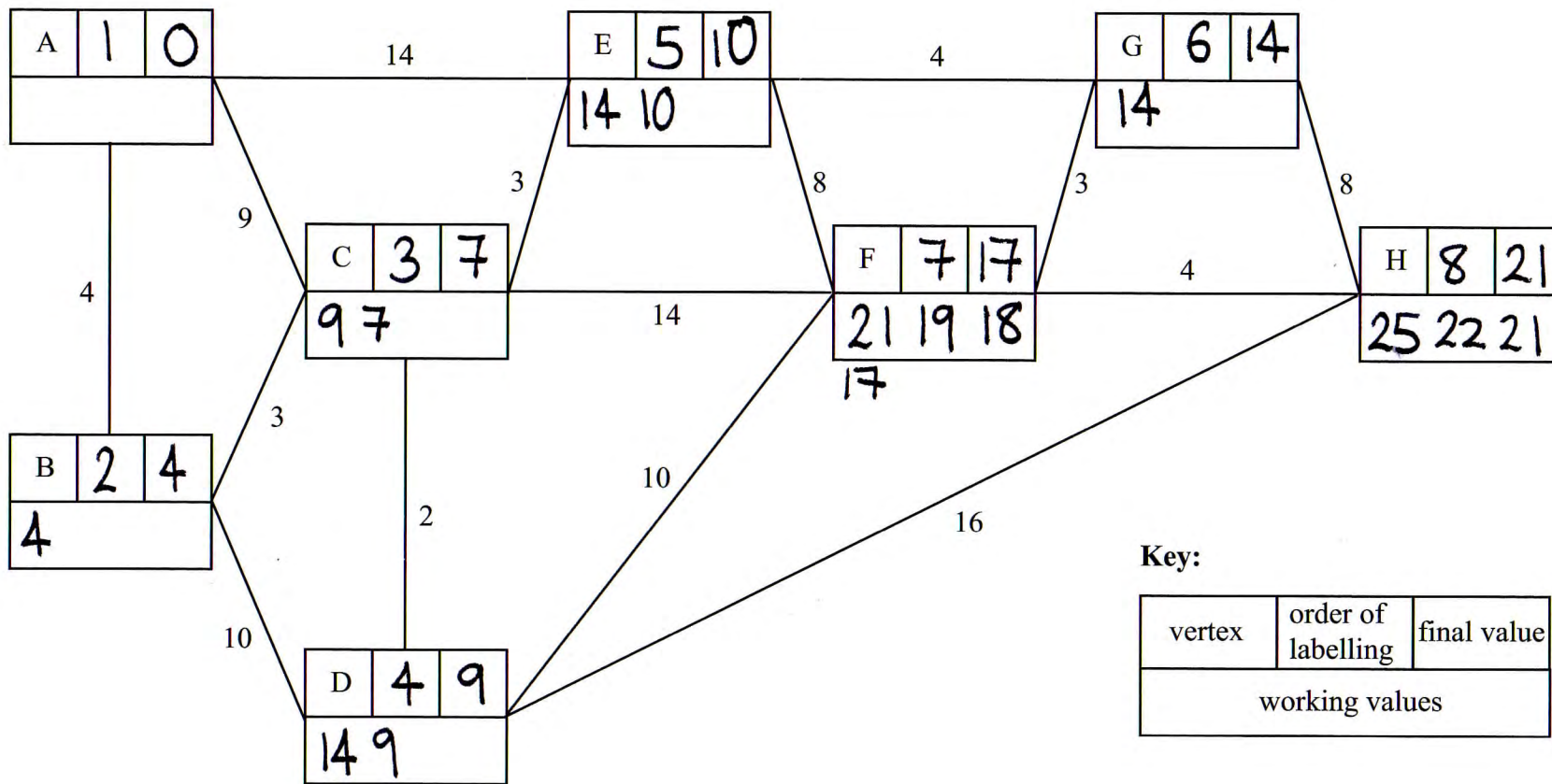


1. (a)



Key:

vertex	order of labelling	final value
working values		

Shortest distance A to H: 21 miles

Question 1 continued

(b)

ABCEGFH

(c)

HFGECL length 14

(Total 8 marks)

Q1

Leave blank



2.

23 29 11 34 10 14 35 17

a) $23+29+11+34+10+14+35+17 = 173$

$\frac{173}{50} = 3.46 \therefore \text{lower bound} = \underline{\underline{4}} \text{ discs}$

Bin1	Bin2	Bin3	Bin4	Bin5
23	29	34	35	17
11	14			
10				

c)

29	23	34	11	14	35	17	10
29	34	23	14	35	17	11	10
34	29	23	35	17	14	11	10
34	29	35	23	17	14	11	10
34	35	29	23	17	14	11	10
35	34	29	23	17	14	11	10

On next pass No swaps so stop.

d)

Bin1	Bin2	Bin3	Bin4
35	34	29	23
14	11	17	10



3.

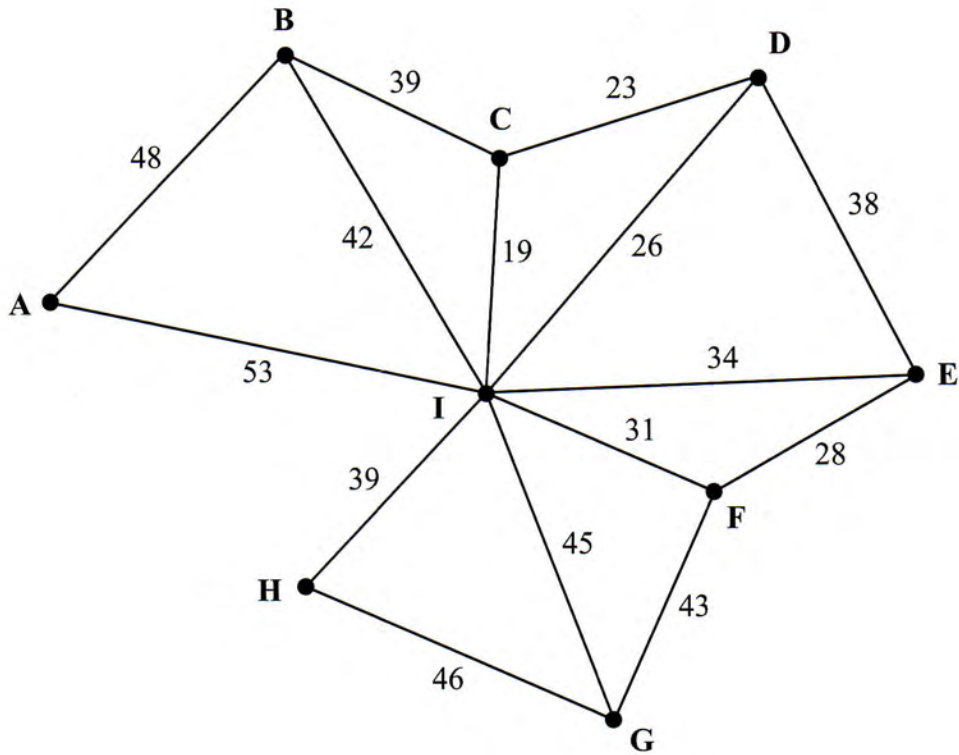


Figure 2

- (a) $CI, CD, DI_{rej}, EF, FI, DE_{rej}, \begin{pmatrix} BC \\ HI \end{pmatrix},$
 $BI_{rej}, FG, IG_{rej}, HG_{rej}, AB$ stop



Question 3 continued

(b) AB, BC, CI, CD, IF, FE, IH, FG

(c)

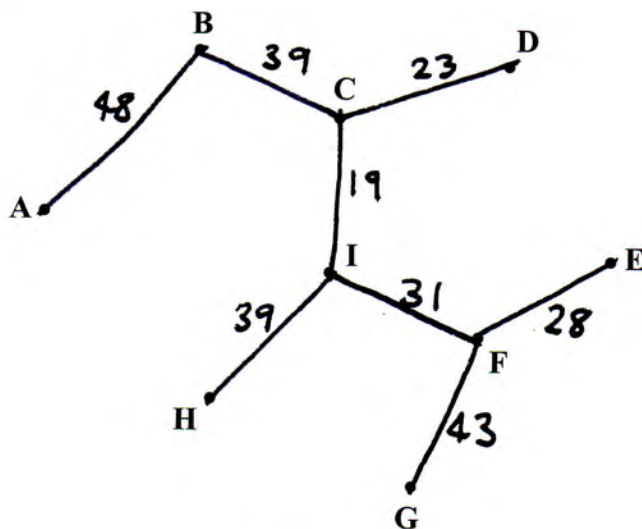


Diagram 1

Weight of minimum spanning tree: 270

(d) Use Kruskal's algorithm. Start by adding DI and HG and then proceed with Kruskal's as normal.

Q3

(Total 10 marks)



4.

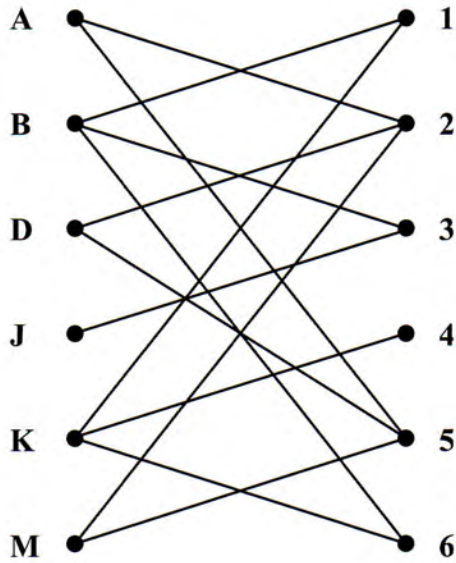


Figure 3

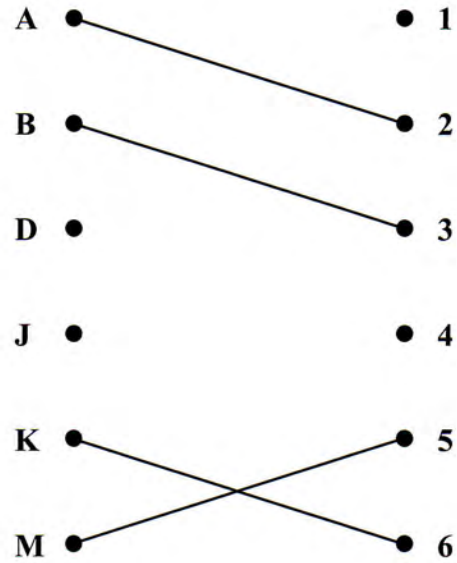


Figure 4

a) Bipartite Graph

b) $J - 3 = B - 6 = K - 4$

c.s

$J = 3 - B = 6 - K = 4$

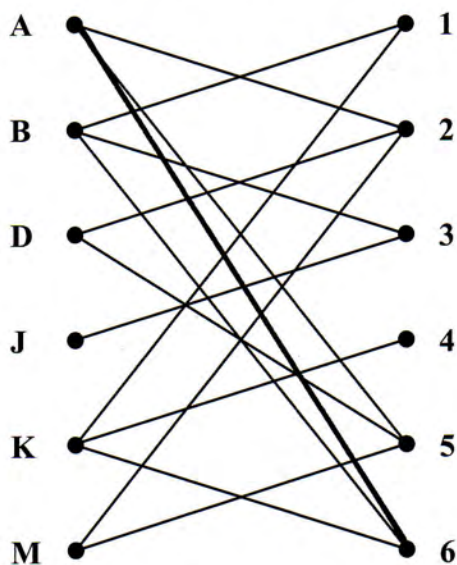
improved matching:

- A = 2
- B = 6
- D
- J = 3
- K = 4
- M = 5

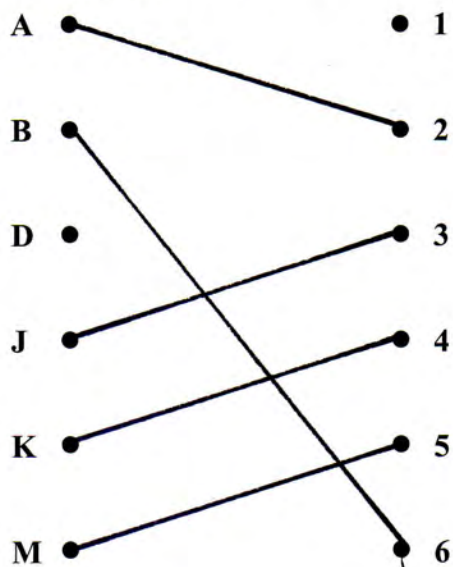
* There are a number of different solutions to this question *



Question 4 continued



initial match



c) $D-2=A-6=B-1$
_{c.s}
 $D=2-A=6-B=1$

complete match :
 $A=6$
 $B=1$
 $D=2$
 $J=3$
 $K=4$
 $M=5$

(Total 7 marks)

Q4



5. a) Odd nodes A, D, F, I

$$AD = 4.5$$

$$AF = 5.8$$

$$AI = 5.9$$

$$FI = 5.3$$

$$DI = 3.9$$

$$DF = 5.1$$

$$\underline{9.8}$$

$$\underline{9.7}$$

$$\underline{11.0}$$

Repeat edges AE, EF and DG, GI

Possible route: ABDGIQDEIHFCAEFEA

b) traverse AE, EF, DG and GI twice

$$\text{length} = 31.6 + 9.7 = \underline{\underline{41.3 \text{ km}}}$$

c) Start at D, finish at A as this leaves FI (FH, HI) to traverse twice length 5.3.

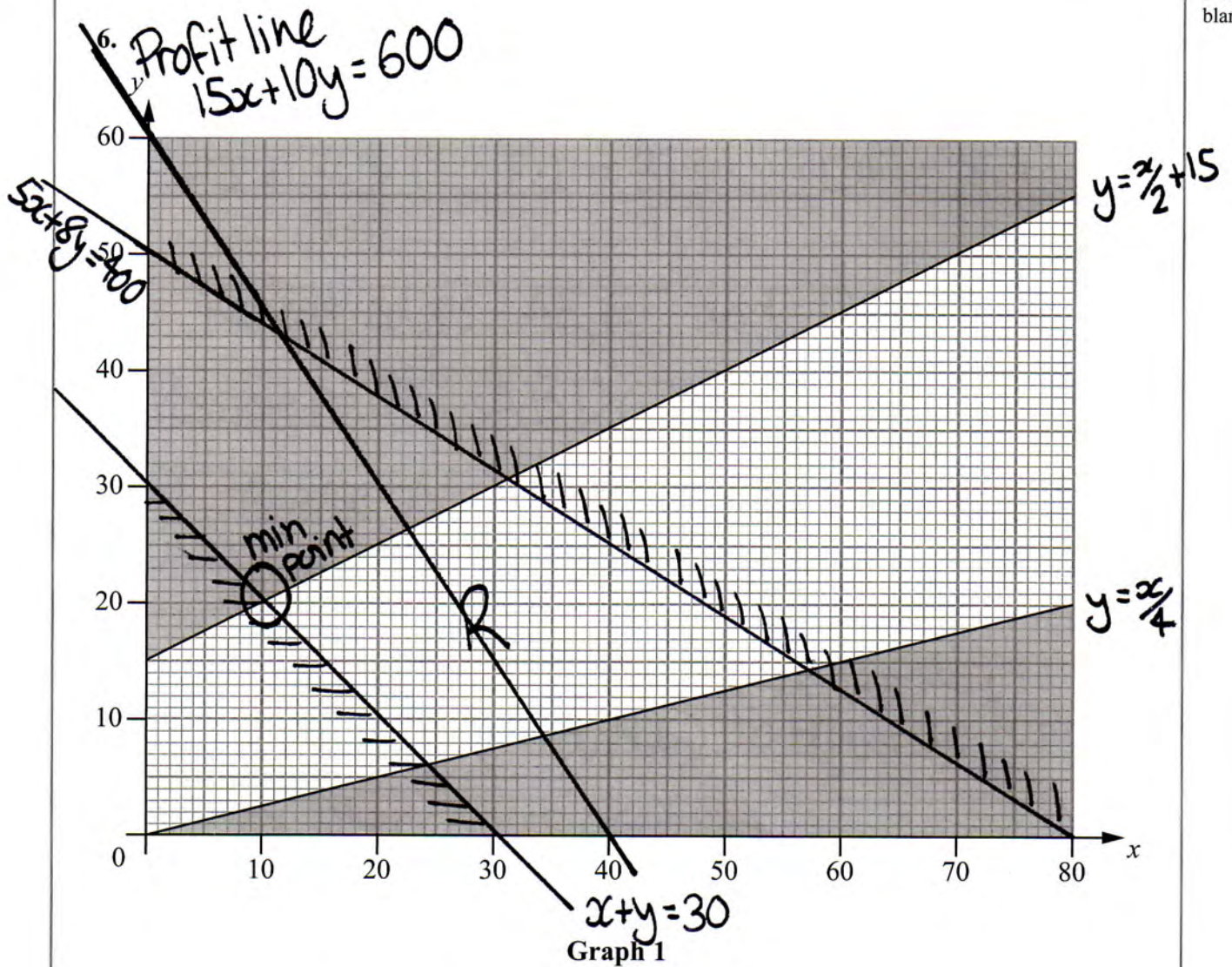
The other choices are:

Finish at I (repeat AF = 5.8)

" " F (repeat AI = 5.9)

both longer than 5.3.





a) $y \leq \frac{x}{4}$ (since grad = $\frac{1}{4}$)
 $y \geq \frac{x}{2} + 15$ (since grad = $\frac{1}{2}$ intercept = 15)

c) min point at (10, 20)

$$\begin{aligned} \therefore \text{Profit} &= 15 \times 10 + 20 \times 10 \\ &= 150 + 200 \\ &= \underline{\underline{350}} \end{aligned}$$



7. (a)

Activity	Immediately preceding activities
A	-
B	-
C	A
D	A
E	A
F	B, C
G	B, C
H	E, F
I	D, E, F
J	H, G
K	I, H, G
L	I, H, G

Precedence table

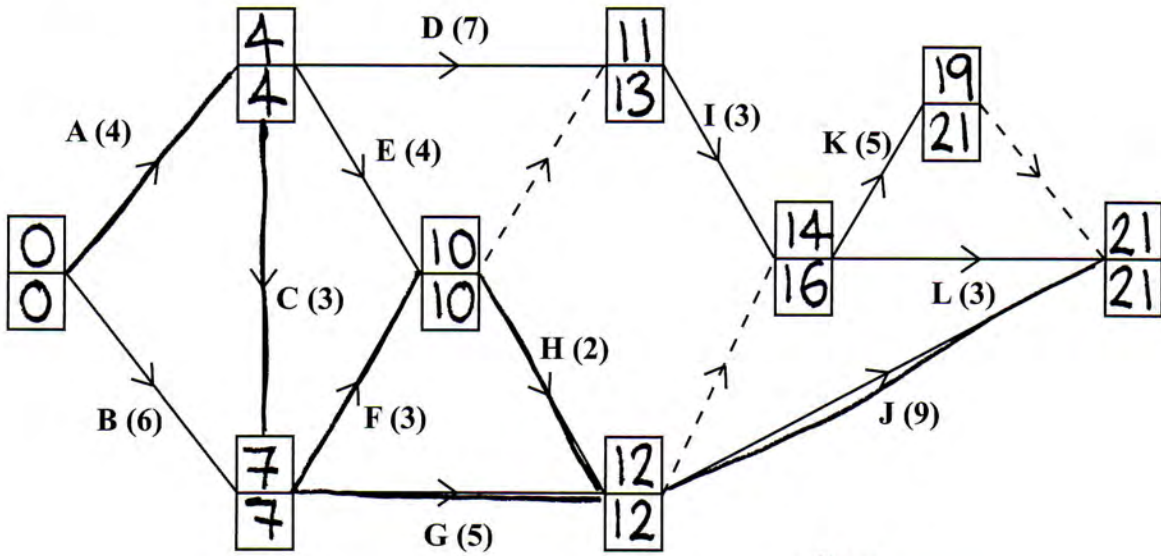
(b) I) To show dependence; K and L depend on I, H and G while J depends on H and G only

II) For uniqueness; each activity must uniquely be expressed in terms of start and end events.



Question 7 continued

(c)



Key:

Early event time
Late event time

Diagram 2

(d) Critical Activities: A, C, (F, H), J

(e) $21 - 5 - 14 = 2$

(f) sum of durations = 54

$\frac{54}{21} = 2.57 \dots \therefore \text{lower bound} = 3$

(Total 16 marks)

Q7

TOTAL FOR PAPER: 75 MARKS

END

